Application

for

United States Letters Patent

To all whom it may concern:

Be it known that,

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has invented certain new and useful improvements in

SYSTEM AND METHOD FOR DETERMINING A SPATIAL HIERARCHY FOR POLYGONAL DATA BY USING CUBE-ROOT SCALING

of which the following is a full, clear and exact description.

SYSTEM AND METHOD FOR DETERMINING A SPATIAL HIERARCHY FOR POLYGONAL DATA BY USING CUBE-ROOT SCALING

CROSS-REFERENCE TO RELATED APPLICATIONS

5   This application claims the benefit of co-pending provisional application Serial No. 60/279,181, filed March 27, 2001 and entitled "SYSTEM AND METHOD FOR ASSIGNING POLYGON BUDGETS, RANGES AND OBJECT SIZES TO A SPATIAL HIERARCHY USING CUBE-ROOT ALTITUDE SCALING."

10   **TECHNICAL FIELD**

The present application relates to determining a spatial hierarchy of polygon data for representing images on a display device. More specifically, the application relates to a system and method for assigning polygon budgets, ranges, object sizes, etc., to a spatial hierarchy by using cube-root altitude scaling.

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DESCRIPTION OF THE RELATED ART

Computer generation of visual scenes is constrained by limitations in data storage and representation of objects in the scenes. A number of image rendering techniques have been proposed.

20   U.S. Patent No. 4,715,005 describes a technique of computer generation of visual scenes of rolling terrain and seascape, using a database of math models. A mathematical formula determines the extent of terrain or sea that must be used to cover a portion of the display. The terrain and sea are modeled using sine waves. There is neither a description nor a suggestion of (i) using a polygonal representation and/or (ii) a hierarchical representation of the data (terrain). There is also no description or suggestion in U.S. Patent No. 4,715,005 of adapting the technique described in the context of terrain and seascape therein to cultural features (such as buildings).

U.S. Patent No. 5,367,615 describes spatial augmentation of vertices and continuous level of detail transition for smoothly varying terrain polygon density, in which the details are statistically derived. There is no description or suggestion in U.S. Patent No. 4,715,005 of adapting the detail processing technique described in the context

of terrain therein to cultural features (such as buildings). There also is neither a description nor a suggestion of deriving range rings mathematically.

SUMMARY

5   The present application provides a system and method for determining a spatial hierarchy for polygon data. The method comprises, in accordance with one embodiment, obtaining a switching range, and determining a polygon density for the spatial hierarchy, by using the switching range and a cube-root scaling factor.

      The method comprises, according to another embodiment, determining a cube-

10   root scaling factor based on an altitude parameter, and using the cube-root scaling factor to scale level-of-detail switching ranges for the spatial hierarchy.

      The methods may be embodied in a computer program (or some unit of code) stored on a computer readable medium, such as a compact disc (CD), and/or transmitted via a computer network, such as the Internet, or another transmission medium.

15   The application also provides a system for determining a spatial hierarchy for polygon data. In one embodiment, the system includes a user interface and a feature analyzer. The feature analyzer determines a polygon density for the spatial hierarchy by using (i) a cube-root scaling factor and (ii) a switch-in distance and switch-out distance obtained through the user interface.

20   The cube-root scaling factor may be determined based on an altitude parameter. The spatial hierarchy may be tile-based. The polygon data may corresponds to cultural feature.

      Design parameters of the spatial hierarchy may be obtained and/or modified through the user interface. For example, one or more of the following may be obtained

25   and/or modified through the user interface: a number of levels in the spatial hierarchy; an extent of tiles for each level of the spatial hierarchy; a critical size of polygonal elements to be inserted in each level of the spatial hierarchy; and a switching distance for tiles of each level of the spatial hierarchy.

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BRIEF DESCRIPTION OF THE DRAWINGS

The features of the present application may be more readily understood from the following detailed description by referring to the accompanying drawings wherein:

FIGS. 1A and 1B show respective two-dimensional graphical representations of

5   a subject band of a computer screen as viewed from a selected eyepoint;

FIG. 2 shows a graphical representation of a vertical field of view;

FIG. 3 shows a graphical representation of vertical density fall-off from the center of a display screen;

FIG. 4 shows a graphical representation of horizontal density fall-off from the

10   center of a display screen;

FIG. 5 shows a graphical representation of a ground range of a tile as a function of altitude, when scaling is turned on;

FIGS. 6A and 6B show graphical representations, in respective additive and substitutive designs, of critical distances for determining object sizes;

15   FIG. 7 shows an Input Sheet in a Point Feature Density Analysis Tool in accordance with one embodiment of the present application;

FIG. 8 shows an Output-TileDesign Sheet in a Point Feature Density Analysis Tool in accordance with one embodiment of the present application;

FIG. 9 shows an Output-FeatureSizes Sheet in a Point Feature Density Analysis

20   Tool in accordance with one embodiment of the present application;

FIG. 10 shows an Output-QuadTree Sheet in a Point Feature Density Analysis Tool in accordance with one embodiment of the present application;

FIG. 11 shows a block diagram of a system, according to one embodiment of the present application, for determining a spatial hierarchy for polygon data;

25   FIG. 12 shows a flow chart of a method, according to one embodiment of the present application, for determining a spatial hierarchy for polygon data; and

FIG. 13 shows a flow chart of a method, according to another embodiment of the present application, for determining a spatial hierarchy for polygon data.

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DETAILED DESCRIPTION

The present application provides new methodologies (for example, in the form of a system and methods) for determining a spatial hierarchy for polygon data for representing images on a display and/or output medium (such as conventional display and output devices). In the spatial hierarchy, the level-of-detail of a displayed feature varies according to the distance between an eyepoint and the feature.

A density computation method provided by the present application may be used, along with a feature prioritization method, to provide selection of source feature data and assignment of geometric models to specific levels-of-detail of the database. The methods provided by the present application may be used to maximize a feature content in a database without exceeding the capacity of the image rendering system. The methods also may be used to achieve a constant polygon density at any elevation. The methods may be adapted for, e.g., flight simulation/visual simulation/geographic database, system or software.

A system 110, in accordance with one embodiment shown in FIG. 11, includes user interface 111, feature analyzer 112 and display monitor 113. Feature analyzer 112 includes a scaling module 112a. User interface 111 and/or feature analyzer 112 may be a computer program stored on a computer readable medium and/or transmitted via a computer network or other transmission medium.

A method, according to one embodiment of the present application, for determining a spatial hierarchy for polygon data will be described with reference to FIGS. 11 and 12. A switching range is obtained through user interface 111 (step 121). A polygon density is determined by feature analyzer 112 using the switching range and a cube-root scaling factor (step 122).

A method, according to another embodiment of the present application, for determining a spatial hierarchy for polygon data will be described with reference to FIGS. 11 and 13. A cube-root scaling factor is determined by feature analyzer 112 based on an altitude parameter obtained through user interface 111 (step 131). Scaling module 112a of feature analyzer 112 uses the cube-root scaling factor to scale level-of-detail switching ranges for the spatial hierarchy (step 132).

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A more detailed description of the system and methods for determining a spatial

hierarchy for polygon data will now be provided.

Given a polygon budget, e.g., corresponding to the storage space in a database,

an ideal polygon density on the ground (assumed to be flat) may be expressed as a

5   function of an altitude of observation z, and the distance d to an eyepoint, as follows:

chaninfo * budget * (z/d^3), where

$$chaninfo = \frac{1}{2\tan\dfrac{FOV_h}{2}(\tan FOV_u + \tan FOV_d)}.$$

10   FOV_h denotes a horizontal field of view, FOV_u denotes an angle above the vertical line

of sight, and FOV_d denotes an angle below the vertical line of sight.

For a given (design) altitude z_0, the equations above may be used to compute an

(ideal) number of polygons that a polygon-tile may contain (depending upon the tile's

switching range and extent).

15   When rendering at an altitude z significantly different from the design altitude z_0,

the polygon budget may be violated, e.g., very few polygons at high altitudes, and too

many at low altitudes. This can be prevented by scaling level-of-detail (LOD) switching

ranges with cube-root scaling, $(z/z_0)^{1/3}$.

20   **1 Analysis in the Continuum**

1.1 Area on the ground corresponding to a horizontal screen band

To compute the polygon density, referring to FIGS. 1A and 1B, a horizontal band

of the computer screen (corresponding to an angle θ as seen from the eyepoint; $t = \tan$

θ) is considered, and the corresponding area of the ground is determined as follows:

25   (1)

$$area(z_0,d) = 2y_0(x_1 - x_0) = 2\tan\frac{FOV_h}{2}\frac{d^3}{z_0}f(p),$$

where FOV_h denotes the horizontal field-of-view, p denotes the pitch angle z_0 the altitude

of the eyepoint, and

$$f(p) = \sin^2 p\left(\frac{1 + t\tan p}{\tan p - t} - \frac{1}{\tan p}\right).$$

The intermediate results are as follows:

5
$$area = 2z_0^2 \cos p \tan \frac{FOV_h}{2}\left(\tan p + \frac{1}{\tan p}\right)\left(\frac{1 + t\tan p}{\tan p - t} - \frac{1}{\tan p}\right),$$

$$\cos p\left(\tan p + \frac{1}{\tan p}\right) = \sin p + \frac{\cos^2 p}{\sin p} = \frac{1}{\sin p} = \frac{\sin^2 p}{\sin^3 p}, \qquad \text{where}$$

$$\sin p = \frac{z_0}{d}.$$

10   Equation (1) can be greatly simplified by choosing a very small θ, thus achieving $t \ll \tan p$, for all pitches (since the existence of a far clipping plane implies that p has a lower bound), such that the following is true:

$$f(p) = \sin^2 p \, \frac{t\tan^2 p + t}{(\tan p - t)\tan p} \approx t.$$
15

For computing a correct polygon density, when intersecting the horizontal field-of-view with the ground, the angle β is actually smaller than FOV_h.

20   **1.2 Polygon density in the continuum**

To determine polygon density, a focal length is first determined from the vertical field-of-view parameters. As explained below, the number of vertical pixels that represent a given object is determined using the focal length.

Referring to FIG. 2, the vertical field-of-view is, in general, non-symmetrical with
25   an angle FOV_u above the vertical line-of-sight and angle FOV_d below the vertical line-of-sight. The following may be determined, with reference to FIG. 2:

vertical no. of pixels = upix + dpix,

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$$focal\ length = upix/tanFOV_u = dpix/tanFOV_d,$$

$$focal\ length = \frac{vertical\ no.\ of\ pixels}{tanFOV_u + tanFOV_d}.$$

To infer density from Equation (1), the number of polygons n assigned to the horizontal screen band (angle θ) is divided with the area of Equation (1).

$$\frac{n}{budget} = t\ \frac{focal\ length}{vertical\ no.\ of\ pixels}$$

The following equation is obtained:

$$density(z,d) = \frac{n}{area(z,d)} = chaninfo \cdot budget \cdot \frac{z}{d^3}.$$

(2)

1.3 Density fall-off and correction

The density in the center of the screen (line of sight) typically is larger than at the periphery. An equal-screen-area vertical band corresponds to a smaller angle at the bottom and top edges of the screen. The overall fall-off for the up field-of-view is as follows, and a similar equation holds for the down field-of-view:

$$\frac{1}{FOV_u} \int_0^{FOV_u} \cos^2\psi d\psi = \frac{1}{2} + \frac{sin2FOV_u}{4FOV_u}.$$

(3)

The total vertical density fall-off is an average of Equation (3) for the up and down fields-of view, weighted by ($tanFOV_u$, $tanFOV_d$). With equal screen length increments (t), the angle corresponding with a screen band reduces with the angle from the center of the screen from θ down to $\theta \cos^2\psi$, as shown in FIG. 3.

Referring now to FIG. 4, at the left and right edges of the screen, the distance to the objects projected on the screen is larger than at the center. The density is thus multiplied by $\cos^3\varphi$. The overall horizon fall-off ($\cos^3\varphi$) is as follows:

$$\frac{2}{FOV_h} \int_0^{\frac{FOV_h}{2}} \cos^3 \varphi d\varphi = \frac{\sin(3FOV_h/2) + 9\sin(FOV_h/2)}{6FOV_h}. \tag{4}$$

The polygon budget may be increased by dividing with the product of Equations (3) and (4). The maximum angle φ in Equation (4) is less than $FOV_h/2$ for a deviation angle ψ from the vertical line of sight different from zero (the tangent of the maximum angle is multiplied by $\cos\psi$). Also, tiling artifacts may alleviate the horizontal fall-off. The density fall-off may be a beneficial phenomenon, assuming that the center of the screen deserves more detail.

2 Analysis for a Hierarchical Tiling System

2.1 Polygon-density for a tile

If (d_1, d_2) denotes the switching range of a tile, and z_0 the design altitude, a suitable density for the tile may be computed by averaging the overall polygon contribution of Equation (2) for the ground area covered between d_1 and d_2, as follows:

$$chaninfo \cdot budget \frac{\int_{d_1}^{d_2} \frac{z_0}{r^3} r dr}{\int_{d_1}^{d_2} r dr} = \frac{2 \cdot z_0 \cdot chaninfo \cdot budget}{d_1 d_2 (d_1 + d_2)}, \tag{5}$$

$$\frac{\frac{1}{d_1} - \frac{1}{d_2}}{d_2^2 - d_1^2} = \frac{1}{d_1 d_2 (d_1 + d_2)}.$$

Integrating over the ground range r is the same as integrating over the slant range (or distance) d, as shown by the following change of variables:

$$\delta r = \delta\sqrt{d^2 - z^2} = \frac{d}{\sqrt{d^2 - z^2}} \delta d = \frac{d}{r} \delta d,$$

$$r\delta r = d\delta d.$$

The polygon budget for the tile may be obtained by multiplying Equation (5) with the area of the tile.

Additive and substitutive tile hierarchies may be considered. In an additive tile hierarchy, the switch-out distance is zero for each tile. When children tiles switch in,
5 they add to the polygon density. The parent is not switched out unless the distance to the tile center becomes larger than the switch-in distance for that tile.

In a substitutive hierarchy, when a tile switches out, the children tiles occupying the void left by the switched-out tile are forced to switch in, *in substitution of* the parent tile. It follows that only the switch-out information is used to determine visibility. The
10 polygon density equation for a substitutive hierarchy is as follows:

$$\frac{2 \cdot z_0 \cdot chaninfo \cdot budget}{d_1 \, d_2 (d_1 + d_2)},$$

where d_1 is the switch-out distance of the tile and d_2 is the "switch-in distance" (switch-out distance of the parent tile).

15 For an additive hierarchy, the same equation is used as a starting point, where d_2 denotes the tile switch-in distance and d_1 denotes the switch-in distance of the next-smaller tile-set, and add to it the cumulative density of all larger tiles (because densities are being added).

20 **2.2   Scaling the LOD switching ranges**

To determine how the switching distances may be "transformed" to match the density curve for z_0 with the density curve for z, a constant density is imposed on Equation (2), and the cube-root scaling is derived directly as follows:

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$$d = d_0 \sqrt[3]{\frac{z}{z_0}}.$$

Equating the altitude with the switch-in distance s_i after it was scaled, the maximum altitude at which a given tile is visible is obtained as follows:

$$z = \sqrt[3]{\frac{z}{z_0}} \, s_i,$$

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$$z = \sqrt{\frac{s_i^3}{z_0}}. \qquad\qquad (6)$$

5   Using cube-root scaling at altitudes significantly smaller than the smaller tile's switch-in radius may not be suitable under some circumstances. For example, cube-root scaling matches ideal density curves, and thus assumes that smaller tiles with yet higher densities are indefinitely available.

   Also, once the altitude is smaller than some fraction of the smallest switch-in

10 radius, all ground ranges increases only minimally when altitude decreases. The polygon counts thus stay approximately constant without scaling. For example, the second observation, the ground range r of the smallest tile may be plotted as a function of altitude as shown in FIG. 5, assuming scaling is turned on, using the following:

15     $$r^2 = (\frac{z}{z_0})^{\frac{2}{3}} s_i^2 - z^2,$$

where s_i is the static (before scaling) switch-in radius of that tile. The altitude corresponding to the largest range, which is obtained by solving for the altitude that sets the derivative of r^2 to zero, is as follows:

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$$\sqrt{\frac{s_i^3}{\sqrt{27}z_0}}.$$

This altitude corresponds to a good clamping altitude for scaling. Below that altitude, scaling reduces polygon counts for all levels simultaneously, with no additional level to

25 fill the gap.

2.3 Recommending sizes for objects populating each set of tiles

   The user defines a MINPIX value, as well as a MAXPIX value, e.g., [1 pixel, 4 pixels]. MINPIX is the smallest size in (vertical) pixels (the channel does not necessarily use square pixels) that an object may be. MAXPIX is the largest size in (vertical) pixels

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an object can be when it switches (or "pops") in and out of the scene.

Consider the following:

$$size[meters] = d \cdot \frac{size[pixels]}{focal\ length}.$$ (7)

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FIGS. 6A and 6B show in respective additive and substitutive schemes the distances for determining suitable object sizes using Equation (7), using MINPIX for d_2 and MAXPIX for d_1. Thus, a minimum and a maximum object size may be determined for all altitudes at which a tile is visible [see Equation (6)].

10   The user may specify the ground range of the smallest tile, e.g., expressed in a factor of the tile's diameter. A number in the vicinity of three is a reasonable choice, which specifies that ten to twenty or so such tiles are visible. The design altitude z_0 may be set to within this ground range, as described above. Scaling works better up than down (limitation of the smallest tile). However, the design altitude cannot be much

15   smaller than this first ground range (providing some up-and-down scaling leverage before having to clamp scaling).

With z_0 determined as described, the first switch-in distance can be determined. Subsequent switch-in distances can be set so as to have approximately the same polygon count in each tile (with potentially some tuning). For example, if the tiles double in size

20   (as in a quad-tree), the density is divided by four, which occurs when multiplying the switch-in distance by $(4)^{1/3} \approx 1.6$ [see Equation (2)].

Cube-root scaling matches exactly the (ideal) density curves at varying altitudes. In order to use a single scale for the entire polygonal database, the polygon-tiles may be designed at the same altitude and Equation (5) used, even if not all tiles are visible, to

25   prescribe a density.

An exemplary embodiment is described below. The embodiment uses a spreadsheet to provide a user interface. It should be understood, however, that other types of user interface may be used also or alternatively. For example, the user interface may be one or a combination of standard, conventional or application specific graphical

30   user interfaces. The user interface may also include voice interface features, which are

also conventionally known and therefore not discussed in detail here.

3 Point Feature Density Analysis Tool

The Point Feature Density Analysis Tool (PFDA) may be provided for specifying

5   a tile-based spatial hierarchy for polygon data representing, e.g., cultural features. The information that may be specified includes the type of hierarchy (additive or substitutive), a number of levels in the hierarchy, an extent of tiles for each level of the hierarchy, and switching distances for tiles of each level. The specified information also may include polygon densities to be applied to each level, a LOD scaling function (which is a function

10   of altitude), and a critical size (described below) of the polygonal elements to be inserted in each level. The PFDA provides a user interface and a feature analyzer. A Point Feature Selection and Allocation Tool (not discussed herein) optionally may be provided for assigning actual features to tiles of a culture hierarchy.

Critical size is the size of a feature as perceived on the display, or difference in

15   sizes between two representations of the same feature. In general, this is the largest dimension of the feature, but other cases may apply depending upon the type of feature. Examples of some special cases include airports, radio towers and other "wireframe" features, and features that are particularly elongated. When substituting models, a measure of the difference between the two models is used.

20   Critical size is used to determine the range at which a model is appropriate in the scene. An extreme example is a model of a house with a textured picture of a door at a low LOD and a polygonal doorframe at a high LOD. The critical size of the high LOD is only ½ inch! Although the door is 7x3 feet, the frame of the door is only relevant when the observer is close enough to discriminate the ½ inch thickness of the door. Critical

25   size is a modeling consideration, and can only be grossly approximated by algorithmic inspection of the model's geometry.

The PFDA may be implemented, according to one embodiment, as an Excel spreadsheet for analyzing point features (buildings, bridges, trees, etc.), but also may provide means for analyzing other visual elements. The PFDA may have a built-in

30   validation step, by which visible tiles are interactively computed for a wide range of

altitudes and lines of sight, to simulate how the polygon budget is utilized under various settings, assuming that recommendations for polygon counts per tile are followed.

FIG. 7 shows an exemplary Input sheet. The following inputs provided by the PFDA may be modified by the user: (a) channel and view information, including horizontal and vertical fields of view, numbers of pixels, depth of view (distance to far clipping plane); (b) tiling scheme definition, including coverage of a geo-cell in meters, number of quad-tree levels, and number of quad-trees in a geo-cell; (c) design parameters, including polygon budget, minimum size of an object on the screen in pixels (*minpix*) and maximum size (*maxpix*) when the corresponding tile switches in or out, and maximum altitude *maxAlt* to which *minpix* and *maxpix* are relevant; and (d) setup for quad-tree display (design validation), including vertical line of sight, elevation, and x,y coordinates of the eyepoint. Once the channel and view information, as well as design parameters, are entered, the bulk of the design work consists of completing the tiling scheme definition.

Design definitions may be entered in cells N3-6. The user specifies the "minimum and maximum size of objects in a tile" (*minpix* and *maxpix*) parameters in cells N3-4. *Minpix* refers to how small any object can be at any time on the screen (generally, one pixel is a reasonable choice). *Maxpix* refers to how large an object can be when it "pops" in and out as its tile switches in or out. If an object is substituted with a different LOD of that object, then the visual difference between the two is what is measured. The polygon budget may be entered in cell N5. The maximum altitude for which *minpix* and *maxpix* are relevant may be entered in cell N6.

Tiling scheme definition may be entered via cells E13-20. The overall coverage size is specified in cells E13-14. The user may choose to divide it in any (integer) number of quad-trees in the x and y directions E15-16.

The number of quad-tree levels may be entered in cell E17, and typically is between 2 and 8. The number of valid levels also may be reflected in output sheets. More levels in the quad-tree yield smaller tiles at the highest LOD and thus also the opportunity for smaller features. This comes at the expense of increased cull depth and larger memory footprint for region files.

The number of tiles in the first range band (highest LOD) may be entered in cell E18, and is a parameter of particular interest. When increasing this number, all the range bands increase in size, following the first band. A finer granularity of the quad-tree is thus obtained, often corresponding to a more graceful matching of the polygon budget. This

5   is obtained at the expense of lower polygon counts per tile, and a larger cull and switching load. Lowering this number causes tile switching to be more aggressive, and therefore increases the likelihood that levels of the hierarchy are skipped in substitutive designs. Quad-Tree simulation provides a visualization of this effect.

The "polygons per tile fall-off ratio" may be entered in cell E19, and used to

10   control the number of polygons per tile for subsequent Quad-Tree LODs. When set to 1, it is approximately constant. When increased, the number of polygons per tile decreases and the sizes of the range bands decreases.

The type of hierarchy (additive =1, substitutive=0) is specified in cell E20. An additive hierarchy causes features to switch in and stay in as the observer approaches.

15   In substitutive hierarchies, features are replaced with higher polygon count versions as the observer approaches. This selection has a major impact on the way density is distributed throughout the scene and the type of models that are used. Quad-Tree simulation provides a visualization of this effect.

A summary of outputs (rows 24 through 35) may be provided on the Input sheet

20   (see FIG 7). Switch range (slant range) for each tile is shown in cells N27-O34 . The switching ranges are subjected to altitude-based scaling performed by the scaling module. The output parameters for scaling in the scaling module are provided in cells N18-19 of the Input sheet. The scaling module scales these values depending upon altitude using the information in N18:20.

25   Cells P27-Q34 show actual polygon budget for each tile and actual density in number of polygons per 1 km square. Using the inputs the user may determine what cumulative density is reasonable. Decreasing the number of Quad-Tree levels (E17), decreases significantly the density of the highest level. Increasing the number of quad-trees in the coverage (E15:16) increases this density. Increasing the number of tiles in

30   the range band of the highest level (E18) decreases the density and the polygons per tile.

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Increasing polygons per tile fall-off ratio (E19) only affects the polygons per tile of the subsequent levels (lower than highest level), but not the polygon count and density of the highest level.

Cells R27-T34 show recommended minimum and maximum object sizes for each tile, based upon the information input in cells N3:N4. If the minimum size exceeds the maximum size, Min > Max appears in the T column. The size distribution is satisfactory if "Min > Max" does not occur, if the range of sizes match the user's data, and if the gaps are not too wide between tiles. Increasing the number of Quad-Tree levels provides a larger distribution and smaller sizes. Increasing the number of Quad-Trees per coverage decreases the sizes globally. Increasing the polygons/tile fall-off ratio may eliminate Min > Max problems, at the expense of fewer polygons in the larger tiles. The same applies to increasing the number of tiles in the range band of the highest level. Again, after changing any of these, the user may press the Quad-Tree Simulation button to validate the new culling load and number of visible tiles.

To validate the number of visible tiles of each type and the number of visible polygons for a given altitude, the Quad-Tree macro may be activated by pressing the "Run QuadTree Simulation" button in cells K25-L25. A graphical display of the visible tiles for the chosen altitude (N9) and line of sight (N10) is then produced in the Output-QuadTree sheet (FIG. 10).

Cells K27-L31 show a summary of the validation/simulation, including a measure of the LOD culling (L28) and frustrum culling (L29) load. The number of visible tiles (L30) and polygons (L31) also may be provided. The number of polygons indicated in cell L31 correspond approximately to the budget, depending upon the altitude (N9), vertical line of sight (N10) and eyepoint location (N12-13). After any change of input data, the "Run QuadTree Simulation" button is activated, so that these numbers may be updated. They are based upon counting visible tiles in the simulation, and do not represent what an actual scene graph may provide.

More detailed output information may be supplied on other sheets, as shown for example in FIGS. 8-10, including the following: (1) polygon counts per tile and tile static switching ranges (Output-TileDesign sheet: FIG. 8); (2) recommended minimum and

maximum feature critical sizes for a range of altitudes (Output-FeatureSizes sheet: FIG. 9) that shows the tiles selected given the input conditions; and (3) graphical validation of the selected design (Output-QuadTree sheet: FIG. 10).

Outputs in the Output-TileDesign Sheet (FIG. 8) will now be described. The

5 static switch ranges (cells A11-18) and polygon counts per tile (G11-18) computed in this worksheet are copied in the Input sheet. The user may override the polygon density equation by typing a number of his/her choice in cells H11-18.

When Quad-Tree validation is performed (triggered by depressing the "Run QuadTree" button in the Input Sheet), validation output is provided, including culling and

10 LOD switching loads (G2,G3), visible tiles (F11-19) and visible polygon counts (I11-19). These visible tiles and polygons are computed using the simulation, but are NOT used for density computations (a general equation is used instead). They depend upon the viewing parameters (altitude, pitch angle, eyepoint x and y locations). The simulation performs tile culling only, as opposed to precise view-frustrum culling. Also, the viewing

15 frustrum may be larger than the working space of the simulation. Therefore, the input polygon budget is not exactly matched in cell I19. Further, the simulation assumes that exact polygon counts (G11-18, or H11-18 when the user decides to override) are applied to each tile, as shown by an artifact of aggregating features into geographic tiles. Varying the simulation's eyepoint location result in aliasing effects in the tile culling process.

20 "Dynamic culture scaling" is enabled within the scaling module.

Outputs in the Output-FeatureSizes Sheet (FIG. 9) will now be described. The lower table (B17-I24) specifies the range of feature critical sizes for the largest LOD-tile level (LOD 1). The *minpix* and *maxpix* input values are transformed into feature critical sizes in meters for a spectrum of altitudes, starting with *maxAlt* as specified in the Input

25 sheet, and decreasing in exponential steps. A size less than cell B24 and larger than cell C17 does not violate a constraint, at all altitudes. The value in cell I17, repeated in cells I18-24, is the geometric mean of cells B24 and C17.

The upper table (B4-I11) applies to other LODs. The user specifies the appropriate LOD number in cell D2. The chart to the right illustrates the minimum and

30 maximum feature critical sizes corresponding to the upper table.

The Output-QuadTree sheet (FIG. 10) provides a graphical layout of visible tiles following level-of-detail and view-frustrum culling, after the "Run QuadTree Simulation" button in the Input sheet is pressed.

The above specific embodiments are illustrative, and many variations can be
5   introduced on these embodiments without departing from the spirit of the disclosure or from the scope of the appended claims. Elements and/or features of different illustrative embodiments may be combined with each other and/or substituted for each other within the scope of this disclosure and appended claims.

For example, additional variations may be apparent to one of ordinary skill in the
10   art from reading U.S. provisional application Serial No. 60/279,181, filed March 27, 2001, which is incorporated herein by reference.